

## What Should I Know About Multiplication and Division Facts?

A goal of the elementary math curriculum is that students master basic multiplication and division facts. Demonstrating mastery of basic facts typically means that you can produce the answer in about 3 seconds or less without resorting to inefficient methods such as counting.

There are three important steps to mastering basic facts. Students need to :

- understand what addition and subtraction mean,
- develop efficient thinking strategies to find the answers,
- and practice using the strategies until the strategies become automatic.

Memorizing basic facts may appear to work for some children. However, students who memorize facts miss out on developing the number sense and reasoning inherent in a strategy approach. The strategies that are used to master the basic facts can be used as mental math strategies for bigger numbers.

## Multiplication and Division Big Ideas

## Multiplication and Addition are Related

Multiplication can be thought of as repeated addition. $6 \times 3$ is the same as $6+6+6$.

## Multiplication and Division are Related

Multiplication and division are inverse operations. If you know $5 \times 4=20$ you also know $20 \div 5=4$.

## Division and Subtraction are Related

Division can be thought of as repeated subtraction. $12 \div 4$ is the same as subtracting groups of 4 until none are left.

## Commutative Property

The order of the factors does not change the product.


When you rotate the array, the number of dots doesn't change, just the way you describe it.

## Multiplication Can Be Modeled Many Ways

## Sets

$3 \times 6$ can be thought of as 3 sets of 6 or 3 groups of 6 .


## Arrays

$3 \times 6$ can be thought of as
3 rows of 6 or 6 rows of 3 .


## Number Lines

$3 \times 6$ can be thought of as
3 jumps of 6 on a number line.

$\begin{array}{lllllll}0 & 3 & 6 & 9 & 12 & 15 & 18\end{array}$

## Numbers are Flexible

Numbers can be broken apart in many different ways. In $4 \times 6$, you can break the six apart several ways to think differently about the problem. You could think of 6 as 3 and 3 , so you multiply $4 \times 3$ $+4 \times 3$. You could also think of 6 as 5 and 1 , so you multiply $4 \times 5$ $+4 \times 1$.

## Basic Fact Strategies

## Twos

Relate to addition doubles


## Tens

Think: Groups of ten


Think: $4 \times 10$ is 4 groups of 10.4 tens is 40 .

## Fives

Relate to Tens: think of a related tens fact and take half of it.


Think: $6 \times 10$ is 60 , half of 60 is 30.

## Zeros and One

Think about groups.
$0 \times 4$ Think: 0 groups of 4 is 0 .
$4 \times 1$ Think: 4 groups of 1 is 4.

## Nines

Relate to Tens: think 10 x and subtract a group.
$9 \times 4$ Think: $10 \times 4$ is 40 , but subtract one group of four, so... 36 .


## Elevens

Relate to Tens: think $10 \times 4$ is 40 , add another set of 4 , so you get 44


## Helping Facts: Fours

Think: Double and double again


Double 6 is 12

Double 12 i= 24

## Helping Facts: Threes

Think: Double and one more set


## Helping Facts: Use a "Close"

 FactThink: Use a "close" fact and add one more set


## Twelves

Think: 10 x and doubles and add them together

$12 \times 4$ Think: $10 \times 4$ is 40 , double 4 is 8 , so $40+8$ is 48 .

## Division as Think Multiplication

Think: Which multiplication fact could help me find an answer?
$35 \div 7$ Think: What times 7 is equal to 35 .

## What Can I Do to Help?

- Use the activity suggestions accompanying the strategies to reinforce each strategy.
- Provide frequent opportunities to practice basic facts. This can be done as you're driving in the car or waiting in line at the grocery store. Flash cards are not needed for practice.
- When your child is unable to provide an answer to a fact within three seconds, ask them to think of a strategy that might help.
- Even when your child can provide an answer quickly, occasionally ask him to explain a strategy that could be used to justify the answer.
- Provide encouragement. Fluency will happen gradually, not overnight.

